# CT Scan for Your Network: Topology Inference from End-to-End Measurements

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#### Network Sciences Research Group (NSRG)

- Interests:
  - communication networking (network tomography, SDN, overlay, 5G, security)
  - distributed machine learning (coreset, data reduction, federated learning)
  - mobile edge computing (resource allocation)
  - cyber-physical systems (smart grid, state estimation, false data injection)
- Members:
  - Ting He, Associate Professor
  - 6 PhD students
  - Alumni: 4 PhD, 6 MS (Bucknell, Google, Meta, ByteDance, HP, Amazon, Oracle)

Network Inference

- Example projects:
- Network tomography



- Software Defined Networks and the software defined Network target
- Communication-efficient ML

**Network Control** 

Data reduction for ML





**PennState** College of Engineering

> ELECTRICAL ENGINEERING AND COMPUTER SCIENCE

## Overview: What is network tomography

• Using *external observations* to infer *internal network state* 



## Motivation: Why topology inference

#### Topology information is useful

- Routing
- Service placement
- Client-server association
- Overlay management
- Load balancing
- Trouble shooting

- But it is not always observable
  - Use protocols to collect topology information (e.g., SNMP, OpenFlow) → admin privilege
  - Use ICMP to measure topology (e.g., traceroute) → supportive internal nodes

• ...

#### Q: Is it possible to infer network topology from end-to-end measurements? If so, how?

## Toy example: Why it is feasible

Multicast measurements reveal internal topology



$$-\log \alpha_1 - \log \alpha_2 = -\log \Pr\{X_{p_1} = 1\},\$$
  
$$-\log \alpha_1 - \log \alpha_3 = -\log \Pr\{X_{p_2} = 1\},\$$
  
$$-\log \alpha_1 = -\log \left(\frac{\Pr\{X_{p_1} = 1\} \Pr\{X_{p_2} = 1\}}{\Pr\{X_{p_1} = X_{p_2} = 1\}}\right).$$

 $X_{p_i}$ : success indicator for path i



### History: Where we are



# Our approach: Revisiting topology inference problems in new application contexts

Restriction on measurement



## Scenario: Probe all paths, arbitrary routing

- Motivation: Inferring the structure and state of <u>SDN-NFV network</u>
  - general topology
  - waypoint traversal
  - known service chain

#### • Observation:

- Measured: end-to-end performance measurements (e.g., losses)
- Inferred: lengths of paths, shared paths, union of paths
  - "length" measured by additive metric
  - E.g.,  $\theta_e = -\log \alpha_e$  ( $\alpha_e$ : success prob. of edge e)
- Static: source, destination, service chain



## Tree-based topology inference is insufficient

- Classic topology inference algorithms all assume tree-based routing
- But trees cannot always reconstruct the observations from a non-tree topology



 $leng(p_1)=4$  $leng(p_2)=6$  $leng(p_3)=3$ 

 $leng(p_1 \cap p_2)=4$ leng(p\_1 \cap p\_3)=1 leng(p\_2 \cap p\_3)=3

No tree topology reconstructs all these lengths  $\rightarrow$  not even guarantee a feasible solution

## Category weights are identifiable

#### • Weight Inference Problem:

- Partition edges into 2<sup>n</sup>-1 *categories* 
  - Category Γ<sub>F</sub>: set of edges *traversed by and only by* paths with indices in F
  - Category weight  $w_F$ : sum metric of edges in category  $\Gamma_F$
- Observe *cast weights*, infer category weights
  - **Cast weight**  $\rho_F$  for a multicast on paths in F:

$$\rho_F \coloneqq -\log(\Pr\{X_F = 1\}) = -\log\left(\prod_{e \in \bigcup_{i \in F} p_i} \alpha_e\right) = \sum_{e \in \bigcup_{i \in F} p_i} \theta_e$$

• Relationship between cast weights and category weights

Topologyagnostic  $\rho_F = \sum_{F' \subseteq E: F' \cap F \neq \emptyset} w_{F'}, \quad \forall F \subseteq E$ 



#### Theorem: Category weights are uniquely determined by cast weights.

## Category weights help, but are not enough

- Under mild assumption, category  $\Gamma_F \neq \emptyset \leftrightarrow w_F \neq 0$
- For trees, knowing non-empty categories → knowing (logical) topology



- But not so for arbitrary topology
  - E.g., can always embed the non-empty categories in a clique-like topology



## Idea: Combining categories with service chain

#### • String Augmentation Problem (SAP):

- view each service chain as a string  $s_i$ ,  $f_{i,1}$ ,  $f_{i,2}$ ,..., $t_i$
- insert dummy letters f<sub>0</sub><sup>1</sup>, f<sub>0</sub><sup>2</sup>,... s.t. for every positive-weight category A, ∃a pair of letters appearing *only* in string i (i∈A)

• Minimize #nodes/#links (can be formulated as an ILP)

## Evaluation: VNF topology inference

• Based on VNF overlays randomly generated on Rocketfuel AS topologies





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# Topology inference from the perspective of upper-layer application

Restriction on measurement



# Overlay Network

- A logical network running on top of an underlying communication infrastructure (underlay network)
  - Enhance best-effort IP-based underlay network
    - Caching, traffic engineering (service-chaining, multicast), fast failover, network slicing, ...
  - Focus: overlay-based routing
- Example: SD-WAN
  - Software-Defined Wide-Area Networks

#### Managed SD-WAN Solutions

AT&T SD-WAN solutions can improve your network's agility and provide centralized control and improve total cost of ownership.







Cisco SD-WAN overlay fabric

## Routing in Overlay Network is Challenging

- Challenges
  - Seemingly independent tunnels share underlay, links
    - Congestion
  - Uncooperative underlay
    - No direct underlay topology information

Q: Do we need the full topology for overlay routing? A: No!



- Flow: a->e and b->d
- Direct tunnel: both traverse  $h_1 \rightarrow h_2$
- Congestion-free overlay routing:
  - a->e
  - b->c->d

## **Overlay Routing Problem**



Q: What is the **minimum information** for **imposing capacity constraints** for an **uncooperative underlay**?

## **Recall: Underlay Link Categorization**

- (Underlay) link category
  - $\Gamma_F(E)$ : A category of links traversed by *F* out of *E* ( $F \subseteq E$ ) is the set of underlay links traversed by and only by the tunnels in *F* out of all the tunnels in *E* 
    - i.e.,  $\Gamma_F(E) \coloneqq \left(\bigcap_{(i,j)\in F} \underline{p}_{i,j}\right) / \left(\bigcup_{(i,j)\in E\setminus F} \underline{p}_{i,j}\right)$ Links shared All links by F traversed by  $E\setminus F$

• Category weight: 
$$w_F(E) \coloneqq \sum_{\underline{e} \in \Gamma_F(E)} \theta_{\underline{e}}$$

Observation: Knowledge of **link categories suffices for congestion-free overlay routing** 



Example:  $E = \{(a, d), (b, e)\}$ 

• 
$$F_1 = \{(a, d), (b, e)\}$$

• 
$$\Gamma_{F_1}(E) = \{(h_1, h_2)\}$$

- $F_2 = \{(a, d)\}$ •  $\Gamma_T (F) = \{(a, h_1), (h_2)\}$ 
  - $\Gamma_{F_2}(E) = \{(a, h_1), (h_2, d)\}$

$$F_3 = \{(b, e)\}$$

•  $\Gamma_{F_3}(E) = \{(b, h_1), (h_2, e)\}$ 

## **Category-based Capacity Constraints**





# **Challenge of Category Inference**



• Full rank linear system

• 
$$w_F(E) > 0 \Longrightarrow \Gamma_F(E) \neq \emptyset$$

#### Q: Is problem solved? A: Unfortunately, **no**

- **Exponential complexity**! #variables =  $2^{|E|} = 2^{O(|V|^2)}$
- Example: |V| = 10, number of candidate categories:  $2^{90}$

## Taming the Complexity in Category Inference

Idea: Given  $\{w_F(E_{t-1})\}$  and  $E_t \leftarrow E_{t-1} \cup \{e_t\}$ , augment it into  $\{w_F(E_t)\}$  $\rightarrow$  Dynamic programming



# Idea for Dynamic Programming

- Category weights are decomposed gradually
  - For any  $E' \subset E$  and  $e \in E \setminus E'$ ,  $w_F(E') = w_{F \cup \{e\}}(E' \cup \{e\}) + w_F(E' \cup \{e\})$

 $E_{t-1} = \{(a, d), (b, e)\}$ 

overlay overlay h<sub>1</sub> underlay underlay  $\{(a, d), (b, e)\}$  $\{(a,d), (b,e), (b,d)\}, \{(a,d), (b,e)\}$  $\{w_F(E_{t-1})\}$  $\{(a, d)\}$  $\{(a,d), (b,d)\}, \{(a,d)\}$  $\{(b, e)\}$  $\{(b,e), (b,d)\}, \{(b,e)\}$  $\{(b, d)\}$  $|supp(w(E_{t-1}))| \leq |\underline{E}|$ 

(#non-empty categories  $\leq$  #underlay links)

 $E_t = \{(a, d), (b, e), (b, d)\}$ 



#variables = 2 $|supp(w(E_{t-1}))| + 1$ 

# Algorithm for Category Inference

- Dynamic programming with the update rule:
  - $E_t \leftarrow E_{t-1} \cup \{e\}$
  - $w_{\{e\}}(E_t) \leftarrow \rho_{E_t} \rho_{E_{t-1}}$
  - For  $F \in supp(w(E_{t-1}))$  in an increasing order of |F|:
    - $w_{F\cup\{e\}}(E_t) \leftarrow \rho_{(E_{t-1}\setminus F)\cup\{e\}} \rho_{E_{t-1}\setminus F} w_{\{e\}}(E_t) \sum_{F' \subset F: F \in supp(w(E_{t-1}))} w_{F'\cup\{e\}}(E_t)$
    - $w_F(E_t) \leftarrow w_F(E_t) w_{F \cup \{e\}}(E_t)$
  - #variables =  $2|supp(w(E_{t-1}))| + 1 = O(|\underline{E}|)$ 
    - In each iteration, solve a **linear system** whose size is **linear in the underlay network size**.
    - In total |*E*| iterations, **linear in the overlay network size**
    - The first **polynomial-time** algorithm for category inference

# Effective Category Capacity Inference

• The minimum capacity of the links in a category may not be measurable



• Effective Category Capacity: maximum flow through the tunnels associated with the category

• 
$$\tilde{C}_F \coloneqq \max_{\substack{(f_e)_{e \in E}}} \sum_{e \in F} f_e \ (f_e: \text{flow assigned to tunnel e})$$
  
s.t.  $\sum_{e' \in F'} f_{e'} \leq C_{F'}, \forall F' \subseteq E, \Gamma_{F'} \neq \emptyset$   
 $f_e \geq 0, \forall e \in E \quad \text{UNKNOWN}$ 

## **Effective Category Capacity Estimation**

#### • Algorithm:

[1] Jain M, Dovrolis C. "End-to-end available bandwidth: measurement methodology, dynamics, and relation with TCP throughput," IEEE/ACM TNET, 2003.

Algorithm 3: Effective Category Capacity Estimationinput : set  $\mathcal{F}$  of category indices of interest (e.g.,<br/> $\mathcal{F} := \{F \subseteq E : \hat{w}_F > \eta\}$ output: Estimated effective category capacities  $\{\hat{C}_F\}_{F \in \mathcal{F}}$ 1 for each  $F := \{e_{i_1}, \cdots, e_{i_{|F|}}\} \in \mathcal{F}$  do2 $f_{e_{i_1}} \leftarrow \hat{C}_{e_{i_1}}(\mathbf{0}); \longrightarrow$  Initialize all flows  $f_e$  to zero3for  $j = 2, \cdots, |F|$  do4 $\int f_{e_{i_j}} \leftarrow \hat{C}_{e_{i_j}}(f); \longrightarrow$  Subroutine [1]: test the residual capacity of a tunnel given flow assignment5 $\hat{C}_F \leftarrow \sum_{j=1}^{|F|} f_{e_{i_j}}; \longrightarrow$  Sum of flow rates6return  $\{\hat{C}_F\}_{F \in \mathcal{F}};$ 

#### • Performance guarantee

- If Line~4 is accurate, then Algorithm 3 achieves  $1/q_F$  approximation
  - $q_F \coloneqq \max_{e \in F} |\{F' \subseteq E : e \in F', \Gamma_{F'} \neq \emptyset, |F' \cap F| > 1\}|$
  - maximum number of nonempty categories a tunnel in F traverses that are shared by at least another tunnel in F

## **Resulting Overlay Routing Problem**



# **NS3-Based Simulation**

#### • Topologies from Internet Topology Zoo

	AttMpls	AboveNet	GTS-CE	BellCanada
$ \underline{V} $	25	23	149	48
<u> </u> <u>E</u>	114	62	386	130
<i>C<u>e</u></i> (Gbps)	1	1	1	1
Link delays (us)	[206,4973]	[100, 13800]	[5,1081]	[78, 6160]

#### • Background traffic

- ON-OFF process for each link independently
  - Duration follows Pareto distribution
  - Utilization: [10%,40%]

#### • Probing

- Number of overlay nodes: 10
- 50-byte packets for probing; 1000-byte packets for routings
- Measurements: end-to-end delays
- Routing cost: link (propagation) delays

## Performance of Inference

#### **Non-Empty Category Detection**

	AttMpls	AboveNet	GTS-CE	BellCanada
#empty cat.	$2^{90} - 69$	$2^{90} - 52$	$2^{90} - 59$	$2^{90} - 51$
#nonempty cat.	69	52	59	51
#false alarms	603	542	2159	1695
#misses	20	27	40	30

- Low false alarm rate although the absolute number is not small
- **High miss rate:** Inaccurate estimation of  $\rho_F$  if (1) |F| is large or (2) tunnels in F have different sources

#### **Effective Category Capacity Estimation**

	AttMpls	AboveNet	GTS-CE	BellCanada
ideal subroutine	0.10%	0.13%	0.13%	0.4%
Pathload	1.07%	1.18%	1.15%	1.49%

• Highly accurate capacity estimation: False alarms will not hurt in most case, but misses may lead to congestions.

## Performance of Overlay Routing

#### Benchmarks

- "Agnostic": an underlay-agnostic routing
- "LCC": the state-of-the-art solution from [2]
- "Proposed"
- "Enhanced proposed": "Proposed" + "LCC"



[2] Y. Zhu and B. Li, "Overlay networks with linear capacity constraints," IEEE TPDS, 2008

**Improved overlay routing performance** despite notable estimation errors



## Concluding Remark

- Topology inference: Jointly infer network internal structure & state from external observations
  - What structures are possible, what measurements are allowed
  - → A tool for application-layer network optimization (e.g., overlay routing)





#### Restriction on measurement

#### CT Scan for Your Network: Topology Inference from End-to-End Measurements

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# Backup slides



#### Restriction on measurement



## Scenario: Passive monitoring only

• A network of independent M/M/1 queues



- Goal: Address two key limitations of existing solutions
  - Active probing → passive monitoring
  - Logical topology → physical topology

### Why it is feasible

- Queue parameter:  $\delta_i = \mu_i \lambda_i$  (residual capacity)
- Sojourn time: exponential r.v. with PDF  $\delta_i e^{-\delta_i t_i}$
- End-to-end delay: hypoexponential r.v. with parameters  $\boldsymbol{\delta} \coloneqq (\delta_i)_{i=1}^K$
- Idea: Queue fingerprinting



# Parameter estimation for tandem of M/M/1 queues: Estimator

h=1

• Idea 1: MLE  
• PDF: 
$$g(x; \delta) = \sum_{i=1}^{K} \delta_i e^{-x\delta_i} \left( \prod_{j=1, j \neq i}^{K} \frac{\delta_j}{\delta_j - \delta_i} \right)$$

- Idea 2: Fitting Laplace transform
  - Laplace transform:  $L(s; \delta) := \prod_{i=1}^{K} \frac{\delta_i}{\delta_i + s}, \quad s > -\min_{i=1,...,K} \delta_i.$
  - Empirical Laplace transform:  $\hat{L}(s; \boldsymbol{x}) := \frac{1}{n} \sum_{k=1}^{n} e^{-sx_{k}}$

$$\rightarrow \qquad \min \quad \sum_{s \in S} |L(s; \, \boldsymbol{\delta}) - \hat{L}(s; \, \boldsymbol{x})| \\ \text{s.t. } 0 < \delta_1 \leq \cdots \leq \delta_K,$$



Parameter estimation for tandem of M/M/1 queues: Performance

• **Theorem.** As  $n \rightarrow \infty$ , Laplace fitting has a unique optimal solution that equals the ground truth  $\delta$  if |S| > K.



## Queueing topology inference: idea



## Queueing topology inference: challenges

- Parameter estimation is not perfect
  - An upper bound  $\Delta$ , such that

 $D_{\{q_{i_1j_1},...,q_{i_kj_k}\}} := \max\{\delta_{i_1j_1},...,\delta_{i_kj_k}\} - \min\{\delta_{i_1j_1},...,\delta_{i_kj_k}\} \le \Delta$ 

- Topology is not arbitrary
  - Partially overlapping categories cannot coexist
- Exponential complexity if brute-forcing
  - $O(K^N)$  ways to merge queues



## Queueing topology inference: solution

- A *greedy* algorithm with *progressively constructed search space* to infer estimated parameters associated with the same queue
  - $O(K^4N^5)$  time complexity,  $O(K^2N^3)$  space complexity
  - Correct if estimated parameters are sufficiently accurate
    - **Theorem.** All parameters for the same queue are correctly identified if  $|\delta_{ij} \delta^*_{ij}| \leq \frac{\Delta}{2} < \frac{\Delta^*}{4}$  (where  $\Delta^* \coloneqq \min_{e \neq e'} |\delta^*_e \delta^*_{e'}|$ )

 $\rightarrow$  Under this condition, the inferred topology will be identical to the ground truth, up to a permutation of queues on the same branch.

### Performance evaluation

Routing trees generated from AS6461 of Abovenet



solid line: edit distance for inferred topology; dotted line: edit distance for multicast tree

#### How to improve the scalability

- Idea: Combining passive & active measurements
  - Passive measurements  $\rightarrow$  queue fingerprints
  - Active measurements  $\rightarrow$  shared path length



## Outline

#### Restriction on measurement



#### Scenario: Cross-path attack

• An attacker in control of a set of *attack paths* wants to launch indirect DoS attack on a set of *target paths* by consuming shared resources

Example 1: Data  $\rightarrow$  Control Plane Attack in SDN

Example 2: Cross-slice Attack in 5G



## Cross-path attack: A high-level description

• Cross-path attack contains a *reconnaissance phase* and an *active attack phase* 

Which attack paths share resource with target paths?WWhat is the capacity of the shared resource?Hc

Which attack paths to use? How much traffic to send?



# Adversarial reconnaissance: A topology inference problem

- Observation model: Active probing on attack paths, passive monitoring on target paths
- Goal: Support optimal attack design
  - Knowing the true routing topology formed by all attack/target paths is sufficient, but not necessary
- Idea: Use mimicked multicast to infer "attack paths + 1 target path" topologies



#### Adversarial reconnaissance: Results

• Recursive algorithm to detect shared links

 Theorem. If all shared links have non-zero metrics and category weights are estimated accurately, then all shared links will be correctly detected.

- Recursive algorithm to estimate parameters of detected shared links
  - Modeled as M/M/1, M/D/1, or G/G/1 queue
  - Estimated by fitting average delay under *K* different probing rates
  - Theorem. If all shared links are correctly detected, and the average delays on target paths are accurately estimated, then the parameters of shared links will be accurately estimated if (i) K > 2 under M/M/1 or M/D/1, and (ii) K > 4 under G/G/1

#### Attack design: Objectives and results

• Objective 1: Delay maximization

$$\begin{split} \max f(\bar{\boldsymbol{\lambda}}) &\coloneqq \sum_{i=1}^{N_B} \beta_i \sum_{e \in \mathcal{T}: W_{ie} > 0} d(\xi_{ie}; \sum_{k=1}^{N_A} h_{ek} \bar{\lambda}_k) \\ \text{s.t.} &\sum_{k=1}^{N_A} \bar{\lambda}_k \leq \lambda, \\ &\sum_{k=1}^{N_A} h_{ek} \bar{\lambda}_k \leq \tilde{r}_e, \ \forall e \in \mathcal{T}, \\ &\bar{\lambda}_k \geq 0, \ k = 1, \dots, N_A, \end{split}$$

• Objective 2: Overload maximization

$$\max_{\bar{\lambda}} \max_{e \in \mathcal{T}: \exists W_{ie} > 0} \left( \sum_{k=1}^{N_A} h_{ek} \bar{\lambda}_k - \min_{i \in \{1, \dots, N_B\}: W_{ie} > 0} r_{ie} \right)$$
  
s.t. 
$$\sum_{k=1}^{N_A} \bar{\lambda}_k \le \lambda, \quad \sum_{k=1}^{N_A} h_{ek} \bar{\lambda}_k \le \tilde{r}_e, \ \forall e \in \mathcal{T}, \quad \bar{\lambda}_k \ge 0, \ k = 1, \dots, N_A,$$

#### Both maximizing convex function under linear constraints

→ Optimum at a vertex
 → If attack rate  $\lambda \le \min_{e \in T} \tilde{r}_e$ , optimal to send all attack traffic on one attack path

### Performance evaluation: NS3 + 5G Lena

• Scenario: 5G IAB (Integrated Access and Backhaul) network



• ON-OFF traffic, discrete packet sizes

#### Performance evaluation: Results



- a) Can detect most of the shared links
- b) Notable error in estimated parameters
- c) Near-optimal performance in attack design

## Concluding Remark

- Topology inference: Jointly infer network *internal structure* from *external observations* 
  - what "internal structure" to infer, what structures are possible, what measurements are allowed
  - → A double-sided sword (overlay management vs. adversarial reconnaissance)







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# Backup slides

#### Example: Shared link detection



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#### Parameter Estimation



Top-down: One queue at a time



M/D/1: 
$$d(\lambda_e, \mu_e; \bar{\lambda}) = \frac{2\mu_e - \lambda_e - \bar{\lambda}}{2\mu_e(\mu_e - \lambda_e - \bar{\lambda})}$$

$$\begin{aligned} \mathsf{G/G/1:} \quad d(\lambda_e, \mu_e, \sigma_{ae}, \sigma_{se}; \bar{\lambda}) \approx \\ \quad \frac{1}{2\mu_e} \frac{\lambda_e + \bar{\lambda}}{\mu_e - \lambda_e - \bar{\lambda}} \Big( \sigma_{ae}^2 (\lambda_e + \bar{\lambda})^2 + \sigma_{se}^2 \mu_e^2 \Big) + \frac{1}{\mu_e} \Big] \end{aligned}$$

Ground truth

#### Parameter Estimation

